

General Physics II for Biological Sciences (Phy 122)

Second Midterm Examination (Fall Semester 2024-2025)

November 23, 2024

Time: 2:00 PM to 3:30 PM

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Solution

$k = \frac{1}{4\pi\varepsilon_0} = 9 \times 10^9 \text{ N} \cdot \text{m}^2/\text{C}^2$ Coulomb's constant $\varepsilon_0 = 8.85 \times 10^{-12} \text{ C}^2/(\text{N} \cdot \text{m}^2)$ Permitivity of free space $\mu_0 = 4\pi \times 10^{-7} \ \mathrm{T\cdot m/A}$ Permeability of free space $e = 1.6 \times 10^{-19} \text{ C}$ Elementary charge $m_e = 9.11 \times 10^{-31} \text{ kg}$ Mass of an electron $m_p = 1.67 \times 10^{-27} \text{ kg}$ Mass of a proton $eV = 1.6 \times 10^{-19} J$ Conversion from eV to J $N_A = 6.022 \times 10^{23}$ /mol Avogadro's number

Prefixes of units					
$m = 10^{-3}$	$\mu = 10^{-6}$	$n = 10^{-9}$	$p = 10^{-12}$	$k = 10^{3}$	$M = 10^6$

Instructions to the Students:

- All communication devices must be switched off and placed in your bag. Anyone found using a communication device will be disqualified.
- Programmable calculators, which can store equations, are not allowed.

Fundamental Constants

1. Three capacitors are connected to a source of emf \mathcal{E} as shown in the circuit. The capacitance $C_1 = C_2 = 9$ nF, but C_3 is unknown. The plate-charges on C_1 and C_3 are $Q_1 = 81$ nC and $Q_3 = 27$ nC respectively.



Solution: We have

$$V_1 = \frac{Q_1}{C_1} = 9 \text{ V}$$

Then

$$\begin{cases} C_2 \text{ and } C_3 \text{ are parallel} \\ C_1 \text{ and } C_{23} \text{ are in series} \end{cases} \implies \begin{cases} Q_1 = Q_{23} \implies Q_1 = Q_2 + Q_3 \\ Q_2 = Q_1 - Q_3 = 54 \text{ nC} \end{cases} \\ \implies V_2 = \frac{Q_2}{C_2} = 6 \text{ V} \\ \implies V_3 = V_2 = 6 \text{ V} \\ \implies C_3 = \frac{Q_3}{V_3} = 4.5 \text{ nF} \\ \implies \mathcal{E} = V_1 + V_{23} = V_1 + V_2 = 15 \text{ V} \end{cases}$$

2. A parallel-plate capacitor with thickness d = 2.7 mm is partially filled with a dielectric of dielectric constant K. The area of the plate above the dielectric is $A_1 = 3.0 \times 10^{-4} \text{ m}^2$ and the area above the empty space (air) between the plates is $A_2 = 4.0 \times 10^{-4} \text{ m}^2$. If the capacitance of this capacitor is C = 4.26 pF, find K.



<u>Solution</u>: This capacitor can be considered as two capacitors C_1 (with the dielectric) and C_2 (with air) in **parallel**. Now

$$C_2 = \varepsilon_0 \frac{A_2}{d} = 1.31 \times 10^{-12} \text{ F}$$

$$C = C_1 + C_2 \implies C_1 = C - C_2 = 2.95 \times 10^{-12} \text{ F}$$

$$C_1 = K\varepsilon_0 \frac{A_1}{d} \implies 2.95 \times 10^{-12} = K\varepsilon_0 \frac{A_1}{d}$$

$$\implies K = 3$$

- 3. A heating coil is required to dissipate 1200 W of power when connected to a 240 V source. If the resistivity of the material of the coil is $\rho = 6.4 \times 10^{-6} \ \Omega \cdot m$ and the radius of the wire is 1.5 mm, find the length of the wire needed to make the coil. **4 points**
 - Solution: We have

$$P = \frac{V^2}{R} \implies R = \frac{V^2}{P} = 48 \ \Omega$$

Then

$$R = \rho \frac{L}{A} \implies L = \frac{RA}{\rho} = \frac{R\pi r^2}{\rho}$$
$$\implies L = 53 \text{ m}$$

4. In the circuit, $R_1 = 20 \Omega$, $R_2 = 24 \Omega$ and $R_3 = 40 \Omega$. The current in is R_1 is $I_1 = 2.4$ A.



Solution: We have

$$V_1 = I_1 R_1 = 48 \text{ V}$$

Then

$$\begin{array}{l} R_2 \text{ and } R_3 \text{ are parallel} \\ R_1 \text{ and } R_{23} \text{ are in series} \end{array} \right\} \implies \begin{cases} R_{23} = \frac{R_2 R_3}{R_2 + R_3} = 15 \ \Omega \\ I_{23} = I_1 = 2.4 \ \Lambda \\ \end{array} \\ \implies V_2 = V_{23} = I_{23} R_{23} = 36 \ V \\ \implies I_2 = \frac{V_2}{R_2} = 1.5 \ \Lambda \\ \implies \mathcal{E} = V_1 + V_{23} = 84 \ V \end{cases}$$

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- 5. In the circuit shown, $R = 12.0 \Omega$, and the emf of the real battery $\mathcal{E} = 20.0 \text{ V}$. When the **switch** S is open the terminal voltage of the battery is 19.2 V.
 - (a) Find the internal resistance of the battery (r). **2 points**
 - (b) Find the terminal voltage of the battery when the switch S is closed. 2 points

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Solution: We see that,

When the switch S is open

$$V_T = \varepsilon - Ir$$
$$\implies Ir = \varepsilon - V_T = 0.8 \text{ V}$$

The equivalent resistance is

$$R_{eq} = R + r \implies I(R + r) = \varepsilon$$
$$IR + Ir = 20 \implies IR = 19.2 \text{ V}$$
$$\implies I = 1.6 \text{ A}$$
$$\implies r = \frac{0.8}{I} = 0.5 \Omega$$

<u>When the switch S is closed</u> The two resistors with $R = 12 \ \Omega$ are parallel. So the equivalent resistance is

$$R_{eq} = \frac{12 \times 12}{12 + 12} + r = 6.5 \ \Omega$$

The current in the circuit is

$$I_1' = \frac{\varepsilon}{R_{eq}} = 3.08 \text{ A}$$

The terminal voltage is

$$V_T' = \varepsilon - I'r = 18.46 \text{ V}$$

6. A proton passes straight through a velocity selector and then enters the mass spectrometer where it moves in circular path of radius R = 3.0 mm. The magnetic fields in the mass spectrometer and the velocity selector are both into-the-plane and have equal magnitude B (see the figure). The magnitude of the electric field is $E = 3.5 \times 10^3$ N/C. Find the **speed** of the proton. **4 points**



Solution: We have

$$E = vB$$
 and $R = \frac{mv}{B|q|} \implies R = \frac{mv^2}{E|q|} \implies v^2 = \frac{E|q|R}{m}$
 $\implies v = \sqrt{\frac{E|q|R}{m}} = 3.17 \times 10^4 \text{ m/s}$

7. Two long straight wires carrying currents perpendicular to the xy-plane are shown. If $I_1 = 6$ A and $I_2 = 5$ A, find B_x and B_y (the <u>x</u>-component and the <u>y</u>-component of the **net magnetic field**) at the point P. **y 6 points**



Solution: We use the Right-Hand rule to draw the directions for $\vec{B_1}$ and $\vec{B_2}$. Then

$$B_{1} = \frac{\mu_{0}I_{1}}{2\pi(0.4)} = 3.0 \times 10^{-6} \text{ T} \implies \begin{cases} B_{1,x} = 0.0 \text{ T} \\ B_{1,y} = -B_{1} = -3.0 \times 10^{-6} \text{ T} \end{cases}$$
$$B_{2} = \frac{\mu_{0}I_{2}}{2\pi(0.5)} = 2.00 \times 10^{-6} \text{ T} \implies \begin{cases} B_{2,x} = +B_{2} \times \frac{0.3}{0.5} = +1.2 \times 10^{-7} \text{ T} \\ B_{2,y} = +B_{2} \times \frac{0.4}{0.5} = +1.6 \times 10^{-6} \text{ T} \end{cases}$$

Then

$$B_x = B_{1,x} + B_{2,x} = +1.2 \times 10^{-6} \text{ T}$$
 $B_y = B_{1,y} + B_{2,y} = -1.4 \times 10^{-6} \text{ T}$

- 8. A uniform magnetic field of magnitude B = 0.8 T in the -x-direction is established in the square shaded area (see figure below). A wire carrying a current I = 7 A passes through this region as shown.
 - (a) Find the magnitude of the magnetic force on the wire.
 - (b) Find the direction of the magnetic force on the wire.

3 points
1 point

The part of the wire lying inside the region of magnetic field has length L such that

$$\frac{0.7}{L} = \cos 30^o \implies L = 0.81 \text{ m}$$

Then, the magnitude of the force is

$$F_B = ILB \sin 30^\circ = 2.26 \text{ N},$$

By the right-hand rule, the direction of the force is **into-the-plane**

