

# **For Instructors use only**

#### Grades:



## **Important**:

- 1. Answer all questions and problems  $\mathcal{N}_0$  solution = no points).
- 2. Full mark = 20 points as arranged in the bove table.
- 3. Give your final answer in the corrections.
- 4. Assume  $g = 10 \text{ m/s}^2$ .
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- 6. Programmable calculators, which can store equations, are not allowed.
- 7. **Cheating incidents will be processed according to the university rules.**

#### **Part I: Short Problems (2 points each)**

**SP1**. A block is moving along the  $x - axis$  under the influence of **a varying net force. The net force as a function of position is shown in the figure. Find the change in the kinetic energy of the block as it moves from**  $x = 0$  **m** to  $x = 8$  **m**.  $F_x(N)$ 

$$
\Delta K = W_{Fnet} = Area
$$

$$
= (4)60) - (4)(40) = +80 J
$$



**SP2.** A constant force F is exerted on a 60 kg block, as shown. The block moves vertically upward at constant speed. Find the average power output of the force  $(F)$  if the block moves  $6m$  in 12 s.

 $W_F = mgh = 60(10)(6) = 3600 J$  $P_{av} =$  $W_F$  $t$ = 3600  $\frac{12}{12}$  = 300 W



**SP3.** A 1000 kg car is moving with **constant speed**, the car encounters a bump in the road that has a circular cross section, as shown. If the apparent weight of the car as it passes over the top is 7000 N, find its **acceleration at the top in unit vector notation.**

 $mg - n = ma_c$  $\Rightarrow a_c =$  $mg - n$  $\boldsymbol{m}$ = 10000 − 7000  $\frac{1000}{1000} = 3 m/s^2$  $\vec{a} = -3\hat{j} \, m/s^2$ 



 $\bf{B}$ 

**SP4.** A box of mass  $m = 2$  kg is attached to a vertical spring  $(k = 100 N/m)$ . The box is released from rest at point A, where the spring is relaxed. The box then moves down from point A to point B, covering a distance of  $s = 0.2$  *m*. Find the speed of the box at point *B*.

$$
\sum W = \Delta K
$$
  
\n
$$
W_{mg} + W_{F_s} = \Delta K
$$
  
\n
$$
mg(s) + \frac{1}{2}k(x_i^2 - x_f^2) = (\frac{1}{2}mv_f^2 - 0)
$$
  
\n
$$
2(10)(0.2) + \frac{1}{2}100(0^2 - 0.2^2) = (\frac{1}{2}(2)v_f^2 - 0)
$$
  
\n
$$
v_f = 1.4 \, m/s
$$

**Or**

$$
E_i = E_f
$$
  
\n
$$
mg(s) = \left(\frac{1}{2}mv_f^2 + \frac{1}{2}kx_f^2\right)
$$
  
\n
$$
2(10)(0.2) = \frac{1}{2}(2)v_f^2 + \frac{1}{2}100(0.2^2)
$$
  
\n
$$
v_f = 1.4 \, m/s
$$

**SP5.** A block of mas  $m$  is sliding down **a frictionless** incline while **a horizontal force** of magnitude  $(F)$  is exerted on it, as shown. If  $F = mg$ , draw the free body diagram of the block and find the angle ( $\theta$ ) of **the incline that allows the block to slide down with constant speed.**

 $mg \sin\theta - F \cos\theta = 0$  $mg \sin\theta = mg \cos\theta$  $sin\theta = cos\theta \Rightarrow tan\theta = 1$  $\Rightarrow \theta = 45^{\circ}$ 



#### **Part II: Long Problems (3 points each)**

**LP1.** Two blocks of wood ( $m_1 = 5$  kg,  $m_2 = 15$  kg), are connected by a light rope and pulled to the right along a horizontal **rough surface** ( $\mu_k = 0.4$ ), as shown.

a) Find the acceleration of the system.



$$
F - \mu_k m_1 g - \mu_k m_2 g = (m_1 + m_2)a
$$
  

$$
a = \frac{F - \mu_k m_1 g - \mu_k m_2 g}{m_1 + m_2} = \frac{120 - (0.4(50)) - (0.4(150))}{20} = 2 m/s^2
$$

b) Find the tension in the rope.

#### **For**

$$
T-\mu_k m_2 g=m_2 a
$$

 $T = \mu_k m_2 g + m_2 a = (0.4)(150) + 15(2) = 90 N$ 

c) Find the magnitude of the **net force** on block 2.

 $F_{net} = m_2 a = 15(2) = 30 N$ 

 $\overline{\star}$   $\overline{\mathbf{A}}$ 

**LP2.** A 30 kg boy starts skating at point A with an initial speed of  $v_A$  and rises to a maximum height of 2 meters above the top of the circular ramp at point C, as shown.

### **a)** Find the boy's speed **at the bottom of the ramp (point B).**

$$
\frac{1}{2}mv_B^2 = mgy_c
$$
\n
$$
v = 0
$$
\n
$$
v = 0
$$
\n
$$
2\,m
$$
\n
$$
v_A
$$
\n
$$
R = 3\,m
$$

b) Find the force exerted by the ramp on the boy **at the bottom of the ramp (point B).**

$$
n_B - mg = m\frac{v^2}{R}
$$
  

$$
n_B = m\left(g + \frac{v^2}{R}\right) = 30\left(10 + \frac{10^2}{3}\right) = 1300 \text{ N}
$$

c) Find the work done on the boy **by gravity** as he moves **from point A to point C.**

$$
W_{mg} = -mgh = -30(10)(2) = -600 J
$$

#### **Part III: Questions (Choose the correct answer, one point each)**

**Q1.** A box of mass *m* rests on **a rough horizontal surface** is being pushed by a horizontal force, as shown. The magnitude of the pushing force  $(\vec{F})$  is increasing **while the box remains at rest**, which of following statements is true about the magnitude of the friction force:

- \* the friction force is constant.
- $(*)$  the friction force is increasing.
- \* the friction force is decreasing.
- \* Impossible to tell without the values of  $m$ ,  $\mu_k$ , and F.

**Q2.** When a box of mass m is released from rest from a height h, its kinetic energy just before touching the ground is K. If a second box of mass  $2m$  is released from rest from the same height  $h$ , then its kinetic energy just before touching the ground is:

 $* K$  $(*)_{2K}$  $*$  4K \* 8



**Q3.** Accelerating a block from  $0 \frac{m}{s}$  to 5  $\frac{m}{s}$  requires a work of magnitude  $W_0$ . Accelerating the same block from  $5 m/s$  to  $15 m/s$  requires the following work:

 $*$  2 $W<sub>o</sub>$  $*$  3 $W_0$  $*$  4 $W_0$  $\bigcirc_{8W}$ 

**Q4.** A ball of mass *m* attached to a light string of length *L* rotates in a vertical circle, as shown. During one **complete revolution**, which of the followings is true regarding **the work done on the ball by force of**  gravity  $(W_q)$ :

\*  $W_q > 0$  $\bigodot W_a = 0$ \*  $W_a < 0$ 

 $*$  Impossible to tell without the values of  $m$  and  $L$ 



