

Askar, Demir, Salameh

For Instructors use only

Grades:

#	SP1	SP2	SP3	SP4	SP5	LP1	LP2	Q1	8	Q3	Q4	Total
	2	2	2	2	2	3	3	1		1	1	20
Pts								4	\leq			
								\overline{Q}	N N			

Important:

- 1. Answer all questions and proble (solution = no points).
- 2. Full mark = 20 points as arrang $\frac{1}{2}$ the above table.
- 3. Give your final answer in the correct units.
- 4. Assume $g = 10 \text{ m/s}^2$.
- 5. Mobiles are **<u>strictly prohibited</u>** during the exam.
- 6. Programmable calculators, which can store equations, are not allowed.
- 7. Cheating incidents will be processed according to the university rules.

GOOD LUCK

Part I: Short Problems (2 points each)

SP1. A constant force $\vec{F} = (30\hat{\imath} - 35\hat{\jmath})$ N acts on a particle that undergoes a displacement of $\vec{s} = (-3\hat{\imath} + 4\hat{\jmath}) m$ in an interval of 4 seconds. Find the average power delivered by \vec{F} during this interval.

$$w = \vec{F} \cdot \vec{S} = (30)(-3) + (-35)(4) = -230 J$$
$$P_{av} = \frac{w}{t} = \frac{-230}{4} = -57.5 W$$

SP2. A ball of mass m = 3 kg attached to a light string of length L = 2 m rotates in a vertical circle, as shown. If the speed of the ball at the bottom of the circle is 6 m/s, find the tension in the rope at this point.





SP3. A 3 kg block rests on a frictionless horizontal surface. <u>A variable</u> force $F(x) = 6x^2 + 4$, where F(x) is measured in N and x is measured in m, starts acting on the block. If the block <u>starts from rest</u> at the origin, use the work-energy theorem to find its speed at x = 2 m.

$$w_{F_x} = \int_{x_i}^{x_f} F_x \, dx = \int_0^2 (6x^2 + 4) \, dx = [2x^3 + 4x]_0^2 = 24 J$$
$$\sum w = w_{F_x} = \Delta K = \frac{1}{2}m \left(v_f^2 - v_i^2\right) = \frac{1}{2}mv_f^2$$
$$\Rightarrow v_f = \sqrt{\frac{2w_{F_x}}{m}} = \sqrt{\frac{2(24)}{3}} = 4 m/s$$

SP4. A block of mass m = 1.2 kg is projected from the top of <u>a frictionless</u> incline with speed v = 5 m/s, as shown. find the speed of the block at the bottom of the incline.

$$E_{f} = E_{i}$$

$$\frac{1}{2} m v_{f}^{2} = \frac{1}{2} m v_{i}^{2} + mgh$$

$$v_{f} = \sqrt{v_{i}^{2} + 2gh} = 9 m/s$$
30°

SP5. A block of mass m = 4.4 kg is held against a wall by a force \vec{F} that makes an angle $\theta = 53.1^{\circ}$ with horizontal, as shown. The coefficient of static friction between the block and the wall is $\mu_S = 0.5$. Find the maximum value of the magnitude of F to prevent the block from sliding up.



Part III: Long Problems (3 points each)

LP1. A block of mass m = 12 kg on a <u>rough horizontal surface</u> is pulled by a rope with tension T = 50 N, as shown. The coefficient of kinetic friction between the block and surface is $\mu_k = 0.3$.

a. Draw a free body diagram for the block.





b. Find the magnitude of the normal force exerted by the surface on the block.

$$n+T\sin(36.9^o)-mg=0$$

$$n = mg - T\sin(36.9^{\circ}) = 12(10) - 50\sin(36.9^{\circ}) = 90 N$$

c. Find the acceleration of the block.

$$T \cos (36.9^{\circ}) - f_k = ma$$

$$T \cos (36.9^{\circ}) - \mu_k n = ma$$

$$a = \frac{T \cos (36.9^{\circ}) - \mu_k n}{m} = 1.1 \ m/s^2$$

LP2 A 2 kg block initially compresses a spring of force constant $k_1 = 1800 N/m$ a distance of $x_1 = 0.2$ m before being released from rest at point A. The block then leaves the spring and slides along a frictionless track until point B, then rough between points B and C. Finally, it compresses another spring of force constant $k_2 = 5000 N/m$ a maximum distance of $x_2 = 0.1 m$.

a. Find the speed of the block when it reaches point B.



$$\frac{1}{2}k_1x_1^2 = \frac{1}{2}mv_B^2 \implies v_B = \sqrt{\frac{k_1}{m}x_1^2} = 6 m/s$$

b. Find the speed of the block when it reaches point C.

$$\frac{1}{2}k_2x_2^2 = \frac{1}{2}mv_c^2 \Rightarrow v_c = \sqrt{\frac{k_2}{m}x_2^2} = 5 m/s$$

c. Find the work done on the block by friction between points B and C

$$w_{f_k} = \frac{1}{2}k_2x_2^2 - \frac{1}{2}k_1x_1^2$$

= $\frac{1}{2}(5000)(0.1^2) - \frac{1}{2}(1800)(0.2^2) = -11J$

OR

$$w_{f_k} = \frac{1}{2}m(v_c^2 - v_B^2) = \frac{1}{2}(2)(5^2 - 6^2) = -11J$$

Part III: Questions (Choose the correct answer, one point each)

- Q1. A book is stationary on a flat, horizontal table. The <u>reaction force</u> to the book's weight is:
 - (*) the gravitational force exerted by the book on the Earth.
 - * the gravitational force exerted by the table on the book.
 - \ast the normal force exerted by the Earth on the book.
 - * the normal force exerted by the table on the book.

Q2. Three masses A, B, and C are connected by a system of massless pulleys and light strings and move as shown in the figure. The <u>work done by the force of gravity on masses A, B, and C respectively</u> is

- * negative, negative, positive
 - * positive, positive, negative
 - * negative, zero, positive
- Positive, zero, negative



Q3. A block is suspended from the ceiling of an elevator by a rope, as shown. If the tension in the rope is greater than the block's real weight, then the elevator moves

* upward with decreasing speed

- (*) downward with decreasing speed
 - * downward with increasing speed
- * upward with constant speed



Q4. Consider the path ABCA shown in the figure. If the work done by a conservative force \vec{F} from A to B is 9 J, and the work done by \vec{F} from B to C is 12 J, then the work done by \vec{F} from C to A is:

 $\begin{array}{c} * & -15 J \\ * & 21 J \\ \bigcirc & -21 J \\ * & 0 J \end{array}$

