**Kuwait University** 



**Physics Department** 



# Important:

- 1. Answer all questions and problems (No solution = no points).
- 2. Full mark = 20 points as arranged in the above table.
- 3. Give your final answer in the correct units.
- 4. Assume  $g = 10 \text{ m/s}^2$ .
- 5. Mobiles and smart watches are **<u>strictly prohibited</u>** during the exam.
- 6. Programmable calculators, which can store equations, are not allowed.
- 7. Cheating incidents will be processed according to the university rules.

# GOOD LUCK

#### Part I: Short Problems (2 points each)

**SP1**. Three forces  $\vec{F}_1 = (50\hat{\imath} - 60\hat{\jmath}) N$ ,  $\vec{F}_2 = (-70\hat{\imath} + 20\hat{\jmath}) N$ , and  $\vec{F}_3$  act on a 4 kg block. If the acceleration of the block is  $\vec{a} = (6\hat{\imath} - 2\hat{\jmath}) m/s^2$ , find  $\vec{F}_3$  in unit vector notation.

$$\sum \vec{F} = m\vec{a}$$
  
$$\vec{F}_1 + \vec{F}_2 + \vec{F}_3 = m\vec{a} \Rightarrow \vec{F}_3 = m\vec{a} - \vec{F}_2 - \vec{F}_3$$
  
$$\vec{F}_3 = 4(6\hat{\imath} - 2\hat{\jmath}) - (50\hat{\imath} - 60\hat{\jmath}) - (-70\hat{\imath} + 20\hat{\jmath}) = (44\hat{\imath} + 32\hat{\jmath}) N$$

**SP2**. The mass of an elevator together with its passengers is 500 kg. At a certain instant, the tension in the supporting cable of the elevator is 6000 N. **Determine the magnitude of its acceleration at this moment.** 

Since  $T > mg \Rightarrow a$  is upward T - mg = ma $\Rightarrow a = \frac{T - mg}{m} = \frac{6000 - 5000}{500} = 2 m/s^2$ 



**SP3.** A 10 kg rock starts sliding on a rough horizontal surface at 8 m/s and stops after 2 s due to <u>a</u> <u>constant</u> frictional force. What average power is produced by friction during the 2 s slide?

$$w_{net} = \Delta K = \frac{1}{2}mv_f^2 - \frac{1}{2}mv_i^2 = -320 J$$
$$P_{av} = \frac{w_{net}}{t} = \frac{-320}{2} = -160 w$$

OR

$$F_{friction} = ma = m\frac{\Delta v}{\Delta t} = 10\left(\frac{8}{2}\right) = 40 N$$
$$P_{av} = \vec{F} \cdot \vec{v}_{av} = -40\left(\frac{8}{2}\right) = -160 w$$

**SP4**. Two blocks  $(m_1 = 5 kg, m_2 = 12 kg)$  are placed on top of each other. Initially, the blocks are at rest, then  $m_2$  is pulled with a horizontal force F and the system starts moving. Find the maximum value of the force  $(F_{max})$  such that  $m_1$  <u>does not slide</u> on  $m_2$ .

## for block 1

$$f_{s_{max}} = \mu_s m_1 g = m_1 a \Rightarrow a = \mu_s g = 7 \ m/s^2$$

for the two blocks

 $F_{max} = (m_1 + m_2) a = 119 N$ 



#### <u>OR</u>

#### (for block 2)

 $F_{max} - f_{s_{max}} = m_2 a \Rightarrow F_{max} = \mu_s m_1 g + m_2 a = 0.7(5)(10) + 12(7) = 119 N$ 

**SP5**. A 0.5 kg box compresses a spring 20 cm at point A, then it is released from rest, as shown. The box slides on a frictionless surface and reaches a circular track of radius R = 2 m, the box leaves the track at point B. Find the spring constant (in N/m).

At point B, 
$$n = 0$$
  
 $\Rightarrow mg \sin(37^{\circ}) = m \frac{v_B^2}{R}$   
 $\Rightarrow v_B = \sqrt{gR \sin(37^{\circ})} = 3.47 \text{ m/s}$ 

$$\frac{1}{2}kx_A^2 = \frac{1}{2}mv_B^2 + mgy_B \Rightarrow k = \frac{m}{x_i^2}(v_B^2 + 2gy_B)$$
$$= \frac{0.5}{0.2^2}(3.47^2 + 2(10)(3.2)) = 950 N/m$$



# Part II: Long Problems (3 points each)

**LP1.** Two blocks ( $m_A = 8 kg$  and  $m_B = 16 kg$ ) on a frictionless horizontal surface are in contact with each other. Two horizontal forces ( $F_1 = 360 N$ , and  $F_2 = 216 N$ ) are applied to the blocks, as shown.

a) Find the magnitude of the acceleration of the system.

$$\sum F = m_{total}a$$
$$360 - 216 = 24 a \Rightarrow a = 6 m/s^2$$



#### b) Find the magnitude of the net force on block B.

$$\sum F_{on\,B} = m_B a = 16(6) = 96\,N$$

# c) Find the magnitude of the contact force between the two blocks.

$$\sum_{AB} F_{on B} = m_B a = F_{AB} - F_2$$
$$F_{AB} = m_B a + F_2 = 96 + 216 = 312 N$$

OR

$$\sum_{F_{on A}} F_{on A} = m_A a = F_1 - F_{BA}$$
$$F_{BA} = F_2 - m_A a = 360 - 8(6) = 312 N$$

**LP2.** A 20 kg block starts moving up **a rough incline** at point A with initial speed  $v_i = 2 m/s$ . It stops momentarily at point **B**. The coefficient of kinetic friction between the block and the incline is  $\mu_k = 0.5$ .

a) Find the total work done on the block as it moves from A to B.



## **b)** Find the distance *d*.

$$\Delta K = w_{total} = w_{f_k} + w_{mg}$$
$$\Delta K = w_{f_k} + w_{mg}$$
$$-40 = -\mu_k mg \cos 37^\circ d - mgd \sin 37^\circ$$
$$d = \frac{40}{mg(\mu_k \cos 37^\circ + \sin 37^\circ)} = 0.2 m$$

# c) Find the change in the gravitational potential energy of the block as it moves from A to B.

$$\Delta U_a = mgy_f - mgy_i = mgd\sin 37^o - 0 = (20)(10)(0.2)\sin 37^o = 24J$$

# Part III: Questions (Choose the correct answer, one point each)

**Q1.** A <u>conservative force</u> is applied to a particle as it moves from point A to point B. If  $W_1$  and  $W_2$  represent

the work done by this force along the paths 1 and 2, respectively then

$$W_1 = W_2 
* W_1 = -W_2 
* W_1 > W_2 
* W_1 < W_2$$





Q3. A ball is released from rest from a height  $h_A$  (point A). It strikes the floor and rebounds to a maximum height  $h_B$  (point B), as shown. The work done on the ball by the gravity ( $W_g$ ) and the corresponding change in total mechanical energy ( $\Delta E$ ) between points A and B are

\*  $W_g > 0 \text{ and } \Delta E = 0$ \*  $W_g < 0 \text{ and } \Delta E = 0$ \*  $W_g < 0 \text{ and } \Delta E < 0$ (\*) $W_g > 0 \text{ and } \Delta E < 0$ 



**Q4.** A block is released from rest at a height *h* above the ground and moves along a **frictionless** surface. If the hills have **the same heights and different radii**, as shown. The relation between the **normal force** exerted on the block at points a, b, and c is:

$$n_a > n_b > n_c$$

$$n_c > n_b > n_a$$

$$n_a = n_b = n_c$$

$$n_b > n_c > n_a$$

