


Second Midterm Examination
Fall Semester 2024 - 2025
November 30, 2024
Time: 11:00 AM – 12:30 PM

Name: Student No:

Section No: Serial No:

Instructors: Drs. Abdullah, Al-Munin, Lajko, Sharma, & Vagenas

Fundamental constants

$k = \frac{1}{4\pi\epsilon_0} = 9.0 \times 10^9 \text{ N}\cdot\text{m}^2 / \text{C}^2$	(Coulomb constant)
$\epsilon_0 = 8.85 \times 10^{-12} \text{ C}^2 / (\text{N} \cdot \text{m}^2)$	(Permittivity of free space)
$\mu_0 = 4\pi \times 10^{-7} \text{ T}\cdot\text{m}/\text{A}$	(Permeability of free space)
$ e = 1.60 \times 10^{-19} \text{ C}$	(Elementary unit of charge)
$N_A = 6.02 \times 10^{23}$	(Avogadro's number)
$g = 9.8 \text{ m/s}^2$	(Acceleration due to gravity)
$m_e = 9.11 \times 10^{-31} \text{ kg}$	(Electron mass)
$m_p = 1.67 \times 10^{-27} \text{ kg}$	(Proton mass)

Prefixes of units

$m = 10^{-3}$	$\mu = 10^{-6}$	$n = 10^{-9}$	$p = 10^{-12}$
$k = 10^3$	$M = 10^6$	$G = 10^9$	$T = 10^{12}$

For use by Instructors only

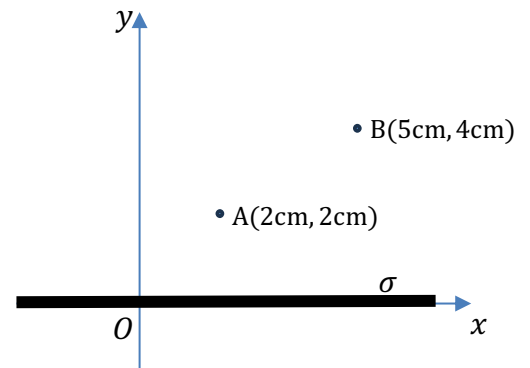
Problems	1	2	3	4	5	6	7	8	Questions	Total
Marks										

Instructions to the Students:

1. Mobile or other electronic devices are **strictly prohibited** during the exam.
2. Programmable calculators, which can store equations, are not allowed.
3. Cheating incidents will be processed according to the university rules.

PART I: Solve the following problems. Show your solutions in detail.

1. An infinite sheet of uniform surface charge density σ is placed perpendicular to the y -axis, as shown. If the potential difference $V_A - V_B$ between the two points A and B is 60 V, find the surface charge density σ . [4 points]



$$d\vec{l} = dx \hat{i} + dy \hat{j}$$

$$\vec{E} = \frac{\sigma}{2\epsilon_0} \hat{j}$$

$$V_A - V_B = \int \vec{E} \cdot d\vec{l}$$

$$V_A - V_B = \int \left(\frac{\sigma}{2\epsilon_0} \hat{j} \right) \cdot (dx \hat{i} + dy \hat{j})$$

$$V_A - V_B = \frac{\sigma}{2\epsilon_0} \int_{0.02 \text{ m}}^{0.04 \text{ m}} dy = \frac{\sigma}{2 \times 8.85 \times 10^{-12}} (0.04 - 0.02) = 60 \text{ V}$$

$$\sigma = 53.1 \text{ nC/m}^2$$

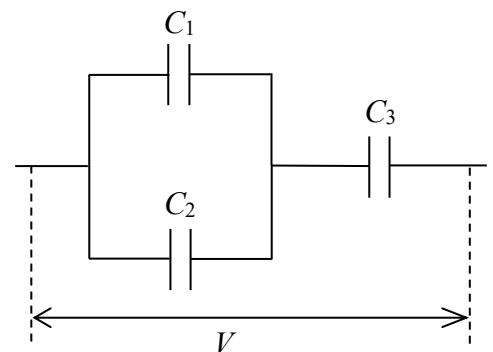
2. In the given network of capacitors with $C_1 = C_2 = 10 \mu\text{F}$ and $C_3 = 20 \mu\text{F}$, the charge on capacitor C_1 is $Q_1 = 20 \mu\text{C}$. Find the charge on capacitor C_3 . [4 points]

$$V_1 = \frac{Q_1}{C_1} = 2 \text{ V} \Rightarrow V_{12} = V_1 = V_2 = 2 \text{ V}$$

$$Q_2 = C_2 V_2 = 20 \mu\text{C}$$

$$Q_{12} = Q_1 + Q_2 = 60 \mu\text{C}$$

$$\text{Since } C_{12} \text{ and } C_3 \text{ are in series, } Q_3 = Q_{12} = 40 \mu\text{C}$$



3. An air-filled parallel-plate capacitor with a surface area A and a plate separation d , has capacitance $C_0 = 20 \mu\text{F}$. The capacitor is partially filled with a dielectric material of dielectric constant $K = 4$, as shown. Find the capacitance C of this arrangement. **[4 points]**

$$C_0 = \epsilon_0 \frac{A}{d}$$

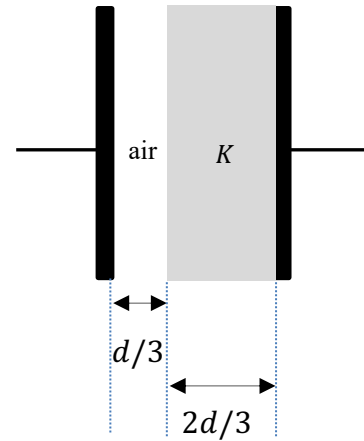
$$C_1 = \epsilon_0 \frac{A}{d/3} = 3\epsilon_0 \frac{A}{d} = 3C_0 = 60 \mu\text{F}$$

$$C_2 = K\epsilon_0 \frac{A}{2d/3} = \frac{3}{2}K\epsilon_0 \frac{A}{d} = \frac{3}{2}4C_0 = 120 \mu\text{F}$$

C_1 and C_2 are in series

$$\frac{1}{C} = \frac{1}{C_1} + \frac{1}{C_2} \Rightarrow \frac{1}{C} = \frac{1}{60 \mu\text{F}} + \frac{1}{120 \mu\text{F}}$$

$$C = 40 \mu\text{F}$$



4. When a cylindrical wire of silver is connected to a battery of 3 V, the power dissipated on it is 15 W. The radius of the silver wire is 0.35 mm and the concentration of free electrons is $5.80 \times 10^{28} \text{ m}^{-3}$. Calculate the drift speed v_d of the electrons. **[3 points]**

$$P = IV \Rightarrow I = \frac{P}{V} \Rightarrow I = 5 \text{ A}$$

$$I = JA \Rightarrow I = n|e|v_d A \Rightarrow I = n|e|v_d \pi r^2$$

$$v_d = \frac{I}{n|e|\pi r^2} \Rightarrow v_d = 1.4 \times 10^{-3} \text{ m/s}$$

5. In the circuit below, find the power dissipated in the internal resistance r_1 .

[3 points]

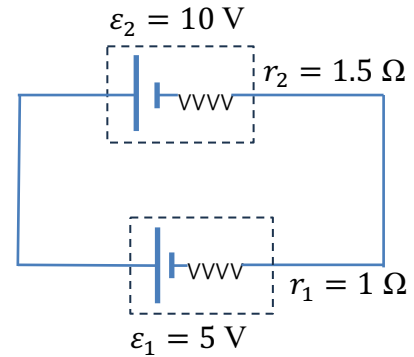
$$V_{term,2} = \varepsilon_2 - Ir_2$$

$$V_{term,1} = \varepsilon_1 + Ir_1$$

$$V_{term,2} = V_{term,1} \Rightarrow \varepsilon_2 - Ir_2 = \varepsilon_1 + Ir_1$$

$$I = \frac{\varepsilon_2 - \varepsilon_1}{r_1 + r_2} \Rightarrow I = 2 \text{ A}$$

$$P_1 = I^2 r_1 \Rightarrow P_1 = 4 \text{ W}$$



2nd solution:

Loop rule (anti-clockwise)

$$10 - 5 - Ir_1 - Ir_2 = 0$$

$$10 - 5 - I - 1.5I = 0 \Rightarrow I = 2 \text{ A}$$

$$P_1 = I^2 r_1 \Rightarrow P_1 = 4 \text{ W}$$

6. In the circuit below, find the equivalent resistance R_{eq} between the terminal points a and b . [4 Points]

R_1 and R_2 are in series:

$$R_{12} = R_1 + R_2 \Rightarrow R_{12} = 10 \Omega$$

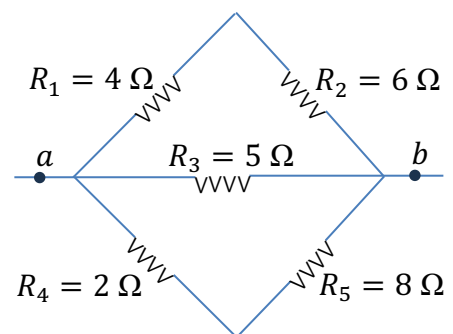
R_4 and R_5 are in series:

$$R_{45} = R_4 + R_5 \Rightarrow R_{45} = 10 \Omega$$

R_{12} , R_{45} , and R_3 are in parallel:

$$\frac{1}{R_{eq}} = \frac{1}{R_{12}} + \frac{1}{R_3} + \frac{1}{R_{45}}$$

$$\frac{1}{R_{eq}} = \frac{1}{10 \Omega} + \frac{1}{5 \Omega} + \frac{1}{10 \Omega} \Rightarrow R_{eq} = 2.5 \Omega$$



7. Find the electric currents I_1 and I_2 , in the circuit below.

[5 Points]

Junction rule: $I_3 = I_1 + I_2$

Loop rules:

Left loop

$$26 - 3I_1 - 7(I_1 + I_2) - 9I_1 = 0$$

$$26 - 19I_1 - 7I_2 = 0 \quad (*)$$

Right loop

$$10 - 5I_2 - 7(I_1 + I_2) - 2I_2 = 0$$

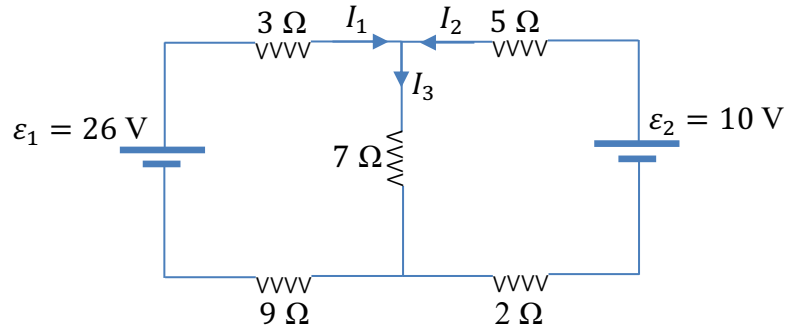
$$10 - 7I_1 - 14I_2 = 0 \quad (**)$$

When we multiply equation (*) with (-2) and add it to equation (**), we get:

$$-42 + 31I_1 = 0 \Rightarrow I_1 = 1.355 \text{ A}$$

Then use equation (1) to calculate I_2 :

$$26 - 19 \times 1.355 - 7I_2 = 0 \Rightarrow I_2 = 0.04 \text{ A}$$



8. The capacitor has an initial charge $Q_0 = 40 \mu\text{C}$ and the switch S is closed at time $t = 0$ s. At time t_1 the charge of the capacitor is half of the initial charge. Find the electric current at the time t_1 . [3 Points]

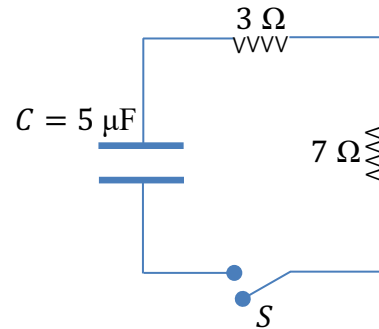
$$R_{eq} = (3 + 7) \Omega = 10 \Omega$$

$$q(t) = Q_0 e^{-\frac{t}{R_{eq}C}} \Rightarrow q(t_1) = Q_0 e^{-\frac{t_1}{R_{eq}C}}$$

$$\frac{Q_0}{2} = Q_0 e^{-\frac{t_1}{R_{eq}C}} \Rightarrow \frac{1}{2} = e^{-\frac{t_1}{R_{eq}C}}$$

$$i(t) = \frac{dq(t)}{dt} = \frac{Q_0}{R_{eq}C} e^{-\frac{t}{R_{eq}C}} \Rightarrow i(t_1) = \frac{Q_0}{R_{eq}C} e^{-\frac{t_1}{R_{eq}C}}$$

$$i(t_1) = \frac{Q_0}{R_{eq}C} \frac{1}{2} \Rightarrow i(t_1) = 0.4 \text{ A}$$



PART II: Conceptual Questions (each carries 1 point). Tick the best answer:

1. Which statement is correct? In electrostatic situation,
 - a) on the outer surface of a charged conductor the electric field is zero.
 - b) inside a charged conductor the electric field is nonzero.
 - c) the full volume of a charged conductor is an equipotential volume. (ANSWER)
 - d) on the outer surface of a charged conductor the electric field is parallel to the surface.
2. An air-filled parallel-plate capacitor with plate separation d , area A , and capacitance C is charged by a battery V and the battery remains connected. If the area A is increased, the electric energy density will
 - a) be zero.
 - b) increase.
 - c) decrease.
 - d) remain the same. (ANSWER)
3. When two identical capacitors are connected parallel with a battery (see Figure 1), their total electric energy is U_1 . When these two identical capacitors are connected in series with the same battery (see Figure 2), their total electric energy, U_2 , will be

- a) $U_1/2$.
- b) $U_1/4$. (ANSWER)
- c) $2U_1$.
- d) $4U_1$.

Figure 1

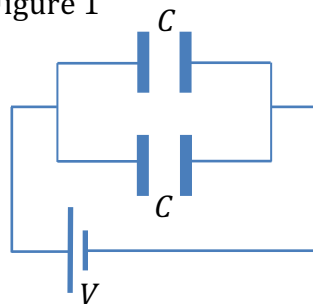
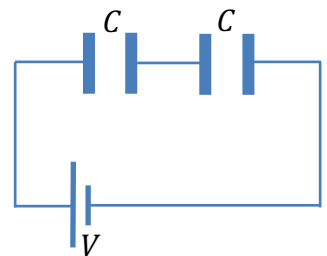
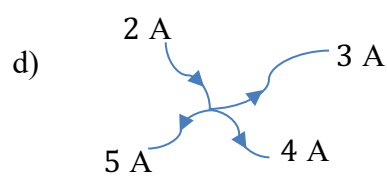
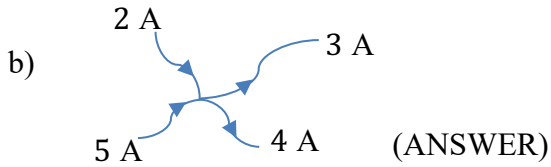
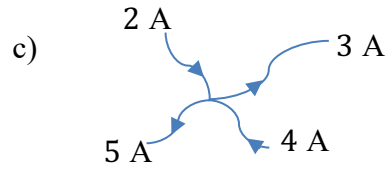
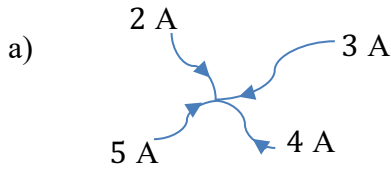


Figure 2



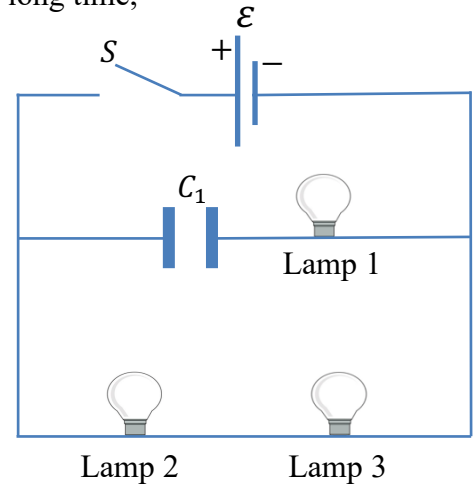
4. The value of the resistivity ρ of a conductor depends
 - a) on the nature of the moving charges in the conductor.
 - b) on the geometrical characteristics of the conductor.
 - c) on the drift speed of the electrons in the conductor.
 - d) on the material and the temperature of the conductor. (ANSWER)

5. At a junction, four wires are met. Which diagram is correct?



6. In the RC circuit, the switch S is closed at $t = 0$ s. After a very long time,

- a) lamps 1, 2, and 3 will light.
- b) lamps 1 and 2 will light but not lamp 3.
- c) lamps 2 and 3 will light but not lamp 1. (ANSWER)
- d) lamps 1 and 3 will light but not lamp 2.



7. In an RC circuit, while a capacitor is charging, the electric current of the circuit

- a) increases exponentially.
- b) decreases exponentially. (ANSWER)
- c) remains the same.
- d) increases and then decreases.

8. In an RC circuit of time constant $\tau = RC$, the capacitor has initial electric charge Q_0 and it starts to discharge at $t = 0$. What fraction of the initial electric charge Q_0 will be on the capacitor at $t = \tau$?

- a) 0
- b) 0.37 (ANSWER)
- c) 0.63
- d) 1.0