

For Instructors use only

Grades:

#	SP1	SP2	SP3	SP4	SP5	LP1	LP2	Q1	80	VQ3	Q4	Total
	2	2	2	2	2	3	3	1		1	1	20
Pts								4	\square			
								\overline{Q}	N N			

Important:

- 1. Answer all questions and proble (solution = no points).
- 2. Full mark = 20 points as arrang $\frac{1}{2}$ the above table.
- 3. Give your final answer in the correct units.
- 4. Assume $g = 10 \text{ m/s}^2$.
- 5. Mobiles are **<u>strictly prohibited</u>** during the exam.
- 6. Programmable calculators, which can store equations, are not allowed.
- 7. Cheating incidents will be processed according to the university rules.

GOOD LUCK

Part I: Short Problems (2 points each)

SP1. Two forces, $F_1 = 25 N$ and $F_2 = 40 N$, act on a 20 kg block that moves on **a frictionless** horizontal surface, as shown. Find the acceleration (in m/s^2) of the block.

$$\sum F_x = ma_x$$

 $F_{1} \cos 37^{o} + F_{2} \cos 60^{o} = ma_{x}$ 25 \cos 37^{o} + 40 \cos 60^{o} = 20a_{x} $a_{x} = 2 m/s^{2}$



E (M)

SP2. A single force F_x acts on a particle, F_x varies with position as shown. Find the total work (in joules) done on the particle as it moves from x = 0 m to x = 4 m.

$$W = Area$$

= (2)(30) + $\frac{1}{2}$ (2)(20) + (2)(10)
= 100 J

SP3. A 7 kg block slides on a semicircular hump of radius R = 21 m, as shown. If the force exerted on the block by the surface at the top of the hump is 58 N, find the speed (in m/s) of the block at the top.

$$mg - n = m\frac{v^2}{R}$$
$$v = \sqrt{\frac{R}{m}(mg - n)} = \sqrt{\frac{21}{7}(7(10) - 58)} = 6 m/s$$



x(m)

 $E_f - E_i = W_{f_k}$

SP4: Two blocks, $m_1 = 5 kg$, and $m_2 = 3 kg$, are pushed vertically up by a force F = 112 N, as shown. Find the magnitude of the force (in newtons) exerted on m_2 by m_1 .

$$F - (m_1 + m_2)g = (m_1 + m_2)a \Rightarrow a = \frac{F - (m_1 + m_2)g}{(m_1 + m_2)} = 4 m/s^2$$

$$F_{12} - m_2g = m_2a \Rightarrow F_{12} = m_2(a + g) = 42 N$$

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SP5. A 4 kg block is released from rest at point A when the spring (k = 3600 N/m) is <u>compressed</u> a distance of x = 0.3 m. The block slides up a rough incline, leaves the spring, and reaches point B with a speed of 5 m/s. Find the coefficient of kinetic friction (μ_k) between the block and the incline.



$$\begin{pmatrix} mgh_B + \frac{1}{2}mv_B^2 \end{pmatrix} - \frac{1}{2}kx^2 = -\mu_k mg\cos(30^o)d \begin{pmatrix} 4(10)(3\sin(30^o)) + \frac{1}{2}(4)(5)^2 \end{pmatrix} - \frac{1}{2}(3600)(0.3)^2 = -\mu_k(4)(10)\cos(30^o)(3) \mu_k = 0.5$$

Part III: Long Problems (3 points each)

- LP1. A 6 kg block starts from rest at point A and moves to point B on a frictionless horizontal surface under the influence of two forces. One force, F_1 , is constant, while the other force, $F_2(x)$, varies according to the equation $F_2(x) = 400x + 60$, where $F_2(x)$ is in newtons and x is in meters. The speed of the block at point B is 12 m/s.
 - a) Find the work done on the block by the force $F_2(x)$ during this motion.



$$W_{F_2(x)} = \int_0^2 (400x + 60)dx = (200x^2 + 60x)]_0^2 = 920 J$$

b) Find the total work done on the block during this motion.

$$W_{total} = \Delta K = \frac{1}{2}m\left(v_f^2 - v_i^2\right) = \frac{1}{2}(6)(12^2 - 0^2) = 432J$$

c) Find the magnitude of the force F_1 .

$$W_{F_1} = W_{total} - W_{F_2(x)} = -488 = (F_1)(s)\cos 127$$

$$F_1 = \frac{W_{F_1}}{s \cos 127^o} = \frac{-488}{2 \cos 127^o} = 405.4 N$$

Fp.

LP2. Two blocks $(m_1 = 20 \ kg$, and $m_2 = 15 \ kg)$ are connected by a light rope that passes over a massless and frictionless pulley, as shown. Block m_1 rests on **a rough** horizontal surface ($\mu_s = 0.6$). A pushing force (F_p) is applied to block m_1 , such that it keeps m_1 at rest and about to move to the left.

a) Find the tension in the rope.

$$m_2g - T = 0$$

 $T = m_2g = 150 N$
 m_1
 m_2

b) Drow the free-body diagram of the block m_1 .



c) Find the magnitude of the pushing force F_p .

$$n = F_p \sin(36.9^o) + m_1 g$$

$$F_p \cos(36.9^\circ) - T - f_{s_{max}} = 0$$

$$F_p \cos(36.9^\circ) - T - \mu_s (F_p \sin(36.9^\circ) + m_1 g) = 0$$

$$F_p = \frac{T + \mu_s m_1 g}{\cos(36.9^\circ) - \mu_s \sin(36.9^\circ)} = 614.4 N$$

Part III: Questions (Choose the correct answer, one point each)

Q1. A block of mass (m) is attached to a spring of force constant (k), the spring is connected to the ceiling, as shown. The block is released **from rest at point A** and comes **momentarily to rest at point B**. The **total work** done on the block between points A and B equals

* mgh
*
$$-\frac{1}{2}kh^2$$

* mgh $+\frac{1}{2}kh^2$
* Zero



Q2. A stone is dropped from the top of a building. As the stone falls, **the instantaneous power delivered by the force of gravity** on the stone

- (*) increases.
- * decreases.
- * stays the same.
- * equals zero.

Q3. A single force is applied to a block along the +x direction, causing it to move on a horizontal frictionless surface along the +x-axis. The magnitude of this force decreases over time. Which of the following statements is correct?

- * The block's acceleration increases with time.
- * The block moves with constant acceleration.
- The block's speed increases with time.
- * The block's speed decreases with time.

Q4. Two boys of **different masses** pull one another using a horizontal light rope, as shown. Each boy applies a force of 230 N on the rope, **but neither boy moves**. Which of the following statements is true?

- * The tension in the rope is 460 N.
- The tension in the rope is 230 N.
- * The force of friction on each boy is 460 N.
- * The heavier boy experiences a larger force of friction.

