

For Instructors use only

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#	SP1	SP2	SP3	SP4	SP5	LP1	LP2	Q1	Q2	- 33	Q4	Total
	2	2	2	2	2	3	3	1	1	1	1	20
Pts												

Important:

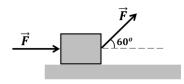
- 1. Answer all questions and problems solution = no points).
- 2. Full mark = 20 points as arranged bove table.
- 3. Give your final answer in the correct nits.
- 4. Assume $g = 10 \text{ m/s}^2$.
- 5. Mobiles are **<u>strictly prohibited</u>** during the exam.
- 6. Programmable calculators, which can store equations, are not allowed.
- 7. Cheating incidents will be processed according to the university rules.

GOOD LUCK

Part I: Short Problems (2 points each)

SP1. A block (m = 6 kg) slides on a **frictionless** surface under the action of two forces, with the same magnitude $|\vec{F}| = 20 N$, as shown. Find the magnitude of the block's acceleration.

 $F + F \cos\theta = ma$ 20 + 20 cos 60° = 6a $a = 5 m/s^2$

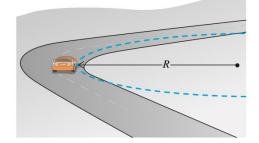


SP2. A car is rounding a flat unbanked curve at a speed of 120 km/h. If the coefficient of static friction of the tire on the road is $\mu_s = 0.6$, what is the minimum radius of the curve such that the car does not slip?

$$F_r = \frac{mv^2}{R}$$

$$F_r = f_{s_{max}} = \mu_s mg = \frac{mv^2}{R}$$

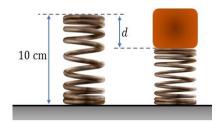
$$R = \frac{v^2}{\mu_s g} = \frac{(120/3.6)^2}{0.6 \times 10} = 185.2 m$$



SP3. A spring of force constant k = 140 N/m and a relaxed length of 10 *cm* is mounted vertically on the ground, as shown. You compress a 150 g block on the spring a distance *d* and release it from rest. Find the value of *d* so that the block reaches a maximum height of 15 cm above the ground?

$$E_i = E_f$$

 $\frac{1}{2}kd^2 = mg(d + 0.05)$
 $d = 0.045 m = 4.5 cm$



SP4. A 10 kg object starts from **the origin** with an initial speed of 3 m/s and undergoes a displacement of $\vec{S} = (5\hat{\imath} + 3\hat{\jmath} + 3\hat{k}) m$, while a net **constant** force $\vec{F} = (-3\hat{\imath} + \hat{\jmath} + 4\hat{k}) N$ acts on it. Use the work-energy theorem and calculate its final speed.

$$w = \vec{F} \cdot \vec{S} = -3(5) + 1(3) + 4(3) = 0 J$$
$$w = \Delta K = \frac{1}{2} m v_f^2 - \frac{1}{2} m v_i^2 = 0$$
So, $v_f = v_i = 3 m/s$

SP5. Consider the following system shown in the figure. The coefficient of static friction between all surfaces is $\mu_s = 0.8$. Find the magnitude of the horizontal force \vec{F} that must be applied to the 4 kg block to just make it move.

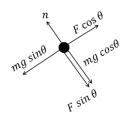


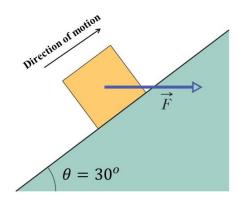
Part II: Long Problems (3 points each)

LP1. A crate of mass m = 100 kg is pushed at <u>constant speed</u> up a frictionless ramp by a horizontal force

 \vec{F} , as shown.

a) Draw the free body diagram of the crate.





b) What is the magnitude of the force \vec{F} ?

For m:
$$\sum F_x = ma = 0$$

$$Fcos\theta - mgsin\theta = 0$$

$$Fcos\theta = mgsin\theta$$

$$F = \frac{mgsin\theta}{cos\theta} = 577.4 N$$

c) What is the magnitude of the normal force exerted on the crate by the ramp?

For m:
$$\sum F_y = 0$$

 $n - Fsin\theta - mg \cos\theta = 0$
 $n = F \sin\theta + mg \cos\theta$
 $n = 577.4 \sin 30^\circ + 1000 \cos 30^\circ = 1154.7 N$

h

LP2. Two blocks ($m_1 = 5 kg$ and $m_2 = 3 kg$) are connected by a light string which passes over a massless pulley, as shown. The block m_1 is connected to a spring of force constant k = 400 N/m on a rough surface. Initially the system is released from rest when the spring is unstretched. The block m_2 descends a distance h = 0.1 m before coming to rest.

a) Find the change in the elastic potential energy during this motion.

$$\Delta U_{el} = \frac{1}{2}kx_f^2 - \frac{1}{2}kx_l^2 = \frac{1}{2}(400)(0.1)^2 - 0 = +2J$$

b) Find the coefficient of kinetic friction between m_1 and the surface.

$$E_f - E_i = W_{other}$$

$$\frac{1}{2}kx_f^2 - m_2gh = -\mu_k m_1gd$$

$$\frac{1}{2}(400)(0.1)^2 - 3(10)(0.1) = -\mu_k(5)(10)(0.1)$$

$$\mu_k = 0.2$$

c) During this motion, the work done on m_2 by the tension in the string is

* positive.

Inegative.

* zero

Part III: Questions (Choose the correct answer, one point each)

Q1. A man exerts a horizontal force to push a box, as shown. In **case I**, the box remains **at rest**, while in case **II**, the box is **about to move**, and in case **III**, the box is moving with **constant speed**. **In which of the three cases the man applies the maximum force**?



Case I The box is at rest.



Case II The box is about to move.



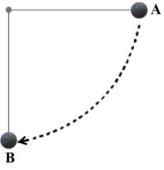
Case III The box is moving at constant velocity.

* The man applies the same force in all cases. * Case I. (*) Case II. * Case III.

Q2. Power has the unit of

* $kg m/s^3$ * $kg m^2/s$ (*) $kg m^2/s^3$ * $kg m^2/s^2$

Q3. A pendulum's bob is released from rest at point A, as shown. The relation between the magnitudes of the accelerations at point B, $|\vec{a}_B|$, and at point A, $|\vec{a}_A|$, is:



Q4. A boy skateboards from rest down a quarter-circle curved rough ramp from point 1 to point 3, where <u>half the way is at point 2</u>, as shown. If the work done on him by friction force from point 1 to point 2 is $W_{f_{1-2}}$ and from point 2 to point 3 is $W_{f_{2-3}}$, then:

$$|W_{f_{2-3}}| < |W_{f_{1-2}}|$$

$$|W_{f_{2-3}}| > |W_{f_{1-2}}|$$

$$|W_{f_{2-3}}| = |W_{f_{1-2}}| = 0$$

$$|W_{f_{2-3}}| = |W_{f_{1-2}}| \neq 0$$

